

Physical Constants

| | | | |
|--------------------------------|-------------------|--|---------------------------------------|
| Newtonian gravitational const. | G | $6.674 \times 10^{-11} \text{ N} \cdot \text{m}^2/\text{kg}^2$ $6.709 \times 10^{-39} \hbar c^5/\text{GeV}^2$ | |
| Avogadro number | N_A | $6.022141 \times 10^{23} \text{ mol}^{-1}$ | |
| Boltzmann constant | k | $1.38065 \times 10^{-23} \text{ J/K}$ | $8.61733 \times 10^{-5} \text{ eV/K}$ |
| speed of light in vacuum | c | $2.99792 \times 10^8 \text{ m/s}$ | |
| reduced Planck's constant | $\hbar(=h/2\pi)$ | $1.05449 \times 10^{-34} \text{ J} \cdot \text{s}$ $6.58151 \times 10^{-22} \text{ MeV} \cdot \text{s}$ | |
| elementary charge | e | $1.6022 \times 10^{-19} \text{ C}$ $4.8032 \times 10^{-10} \text{ esu}$ | $1.6022 \times 10^{-20} \text{ emu}$ |
| electron mass | m_e | $9.10938 \times 10^{-31} \text{ kg}$ | $0.5109989 \text{ MeV}/c^2$ |
| unified atomic mass unit | u | $1.660539 \times 10^{-27} \text{ kg}$ | $931.4941 \text{ MeV}/c^2$ |
| vacuum permittivity | ϵ_0 | $8.854187817 \times 10^{-12} \text{ F/m}$ | electric constant |
| Fermi coupling constant | $G_F/(\hbar c)^3$ | $1.16638 \times 10^{-5} \text{ GeV}^{-2}$ | |
| Fine structure constant | α | 0.00729735257 | $(137.036)^{-1}$ |

Unit Conversion

| | |
|------------------|----------------------------|
| 1 inch = 2.54 cm | 1 pound(lb) = 0.4535923 kg |
| 1 cal=4.185 J | |

Dimensions (suffix denotes power of energy in natural unit with H-L and $k = 1$)

| | | | |
|-----------------------------------|-----------------------------|---|-----------------------------|
| Length (m) | $[L]_{-1}$ | Mass (kg) | $[M]_1$ |
| Time (s) | $[T]_{-1}$ | Current (A) | $[J]_1$ |
| Momentum (N·s) | $[MLT^{-1}]_1$ | Force (N) | $[MLT^{-2}]_2$ |
| Work (J) | $[ML^2T^{-2}]_1$ | Angular momentum | $[ML^2T^{-1}]_0$ |
| Power (W) | $[ML^2T^{-3}]_2$ | (N·m·s) | |
| Moment (N·m) | $[ML^2T^{-2}]_1$ | Moment of inertia | $[ML^2]_{-1}$ |
| Pressure (Pa=N/m ²) | $[ML^{-1}T^{-2}]_4$ | (kg·m ²) | |
| Permittivity ϵ (F/m) | $[M^{-1}L^{-3}T^4J^2]_0$ | Charge (C) | $[TJ]_0$ |
| Electric field strength E (V/m) | $[MLT^{-3}J^{-1}]_2$ | Electric flux density D (C/m ²) | $[L^{-2}TJ]_2$ |
| Electric potential (V) | $[ML^2T^{-3}J^{-1}]_1$ | Electric capacity (F) | $[M^{-1}L^{-2}T^4J^2]_{-1}$ |
| Electric resistance (Ω) | $[ML^2T^{-3}J^{-2}]_0$ | Permeability μ (H/m) | $[MLT^{-2}J^{-2}]_0$ |
| Magnetic charge (Wb) | $[ML^2T^{-2}J^{-1}]_0$ | Magnetic field strength H (A/m) | $[L^{-1}J]_2$ |
| Magnetic vector potential | $[MLT^{-2}J^{-1}]_1$ | | |
| Magnetic flux density B (T) | $[MT^{-2}J^{-1}]_2$ | Magnetic flux Φ (Wb = T·m ²) | $[ML^2T^{-2}J^{-1}]_0$ |
| Inductance (H=Wb/A) | $[ML^2T^{-2}J^{-2}]_{-1}$ | | |
| Temperature (K) | $[\theta]_1$ | Expansion coefficient (K ⁻¹) | $[\theta^{-1}]_{-1}$ |
| Thermal capacity (J/K) | $[ML^2T^{-2}\theta^{-1}]_0$ | | |
| Thermal conductivity (W/m·K) | $[MLT^{-3}\theta^{-1}]_2$ | Entropy (J/K) | $[ML^2T^{-2}\theta^{-1}]_0$ |

Electromagnetic Units

$$\begin{aligned}
 \vec{F} &= q\vec{E} & \vec{F} &= m\vec{H} & \frac{\partial\rho}{\partial t} + \nabla \cdot \vec{j} &= 0 \\
 \vec{F} &= \frac{1}{h_1\epsilon_0} \frac{qq'\vec{r}}{r^2} & \vec{F} &= \frac{1}{h_2\mu_0} \frac{mm'\vec{r}}{r^2} & \vec{F} &= \frac{1}{h_3k} \frac{m\vec{j} \times \vec{r}}{r^3} \\
 \Rightarrow \nabla \cdot \vec{E} &= \frac{4\pi}{h_1\epsilon_0} \rho & \nabla \times \vec{H} &= \frac{4\pi}{h_3k} \vec{j} + \frac{h_1\epsilon_0}{h_3k} \frac{\partial\vec{E}}{\partial t} & \nabla \times \vec{E} &= -\frac{h_2\mu_0}{h_3k} \frac{\partial\vec{H}}{\partial t} \\
 \vec{F} &= q\vec{E} + \frac{h_2\mu_0}{h_3k} q\vec{v} \times \vec{H} : \text{Lorentz force} & & & \frac{h_3^2}{h_1h_2} \frac{k^2}{\mu_0\epsilon_0} &= c^2 \\
 S &= \frac{h_3k}{4\pi} \vec{E} \times \vec{H} & E &= \frac{1}{8\pi} (h_1\epsilon_0\vec{E}^2 + h_2\mu_0\vec{H}^2) & \alpha &= \frac{e^2}{h_1\epsilon_0\hbar c}
 \end{aligned}$$

| | MKSA | esu | emu | Gauss | Heaviside-Lorentz |
|---------------------------|--|--|--|---|--|
| $h_1 = h_2 = h_3 =$ | 4π | 1 | 1 | 1 | 4π |
| ϵ_0 | $\frac{1}{\mu_0 c^2}$ | 1 | $\frac{1}{c^2}$ | 1 | 1 |
| μ_0 | $\frac{4\pi}{10^7}$ | $\frac{1}{c^2}$ | 1 | 1 | 1 |
| k | 1 | 1 | 1 | c | c |
| $\nabla \cdot \vec{D} =$ | ρ | $4\pi\rho$ | $4\pi\rho$ | $4\pi\rho$ | ρ |
| $\nabla \cdot \vec{B} =$ | 0 | 0 | 0 | 0 | 0 |
| $\nabla \times \vec{H} =$ | $\vec{j} + \frac{1}{c} \frac{\partial\vec{D}}{\partial t}$ | $4\pi\vec{j} + \frac{\partial\vec{D}}{\partial t}$ | $4\pi\vec{j} + \frac{\partial\vec{D}}{\partial t}$ | $\frac{4\pi}{c} \vec{j} + \frac{1}{c} \frac{\partial\vec{D}}{\partial t}$ | $\frac{1}{c} \vec{j} + \frac{1}{c} \frac{\partial\vec{D}}{\partial t}$ |
| $\nabla \times \vec{E} =$ | $-\frac{\partial\vec{B}}{\partial t}$ | $-\frac{\partial\vec{B}}{\partial t}$ | $-\frac{\partial\vec{B}}{\partial t}$ | $-\frac{1}{c} \frac{\partial\vec{B}}{\partial t}$ | $-\frac{1}{c} \frac{\partial\vec{B}}{\partial t}$ |
| $\vec{D} =$ | $\epsilon\vec{E}$ | $\frac{\epsilon}{\epsilon_0} \vec{E}$ | $\frac{\epsilon}{\epsilon_0 c^2} \vec{E}$ | $\frac{\epsilon}{\epsilon_0} \vec{E}$ | $\frac{\epsilon}{\epsilon_0} \vec{E}$ |
| $\vec{B} =$ | $\mu\vec{H}$ | $\frac{\mu}{\mu_0 c^2} \vec{H}$ | $\frac{\mu}{\mu_0} \vec{H}$ | $\frac{\mu}{\mu_0} \vec{H}$ | $\frac{\mu}{\mu_0} \vec{H}$ |

Natural Units with Heaviside-Lorentz

$$\hbar = c = 1 \quad \epsilon_0 = \mu_0 = 1 \quad [L^{-1}] = [T^{-1}] = [M] = [J] = [\mathcal{E}(ML^2T^{-2})]$$

$$\hbar c = 197 \text{ MeV} \cdot \text{fm}$$

$$1 \text{ kg} = 5.61 \times 10^{29} \text{ MeV} \quad 1 \text{ MeV} = 1.60 \times 10^{-13} \text{ J} = 1.78 \times 10^{-30} \text{ kg} \cdot c^2$$

$$1 \text{ J} = 6.24 \times 10^{12} \text{ MeV}$$

$$1 \text{ s} = 3.00 \times 10^{23} \text{ fm} = 1.52 \times 10^{21} \text{ MeV}^{-1} \quad 1 \text{ s}^{-1} = 6.58 \times 10^{-22} \text{ MeV}$$

$$1 \text{ m} = 5.07 \times 10^{12} \text{ MeV}^{-1}$$

$$1 \text{ N} = 1.23 \text{ MeV}^2$$

$$\frac{e^2}{4\pi\epsilon_0\hbar c} \rightarrow \frac{e^2}{4\pi} = \frac{1}{137} \quad e = \sqrt{4\pi/137} = 0.303$$

$$1 \text{ C} = 1.89 \times 10^{18} \quad 1 \text{ V} = 3.30 \text{ eV} \quad 1 \text{ V/m} = 6.52 \times 10^{-19} \text{ MeV}^2$$

$$1 \text{ A} = 1.24 \times 10^{-3} \text{ MeV} \quad 1 \text{ T} = 1.95 \times 10^{-10} \text{ MeV}^2$$